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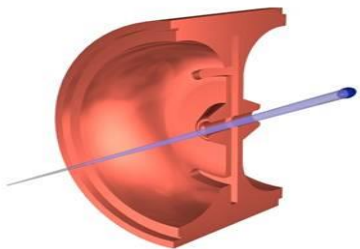


# Low-Alpha Storage Ring Design for Steady-State Microbunching to generate EUV radiation

On behalf of Tsinghua SSMB team

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Accelerator Laboratory of Tsinghua University

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- Introduction
- Linear lattice design
- Nonlinear study
- Summary



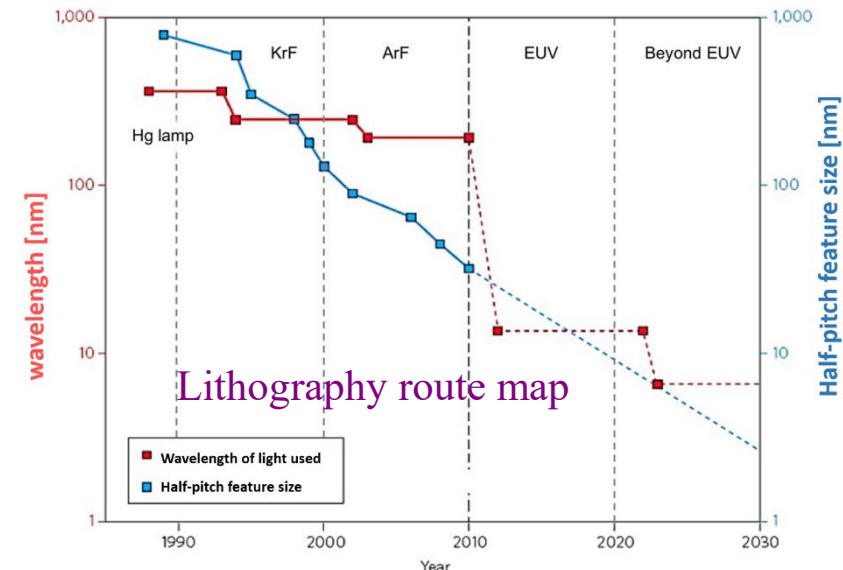
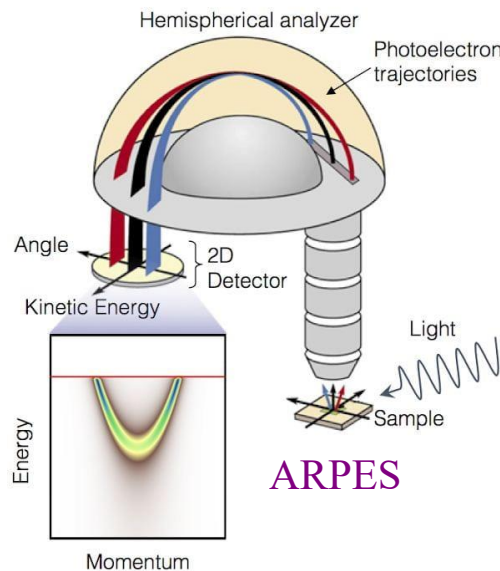
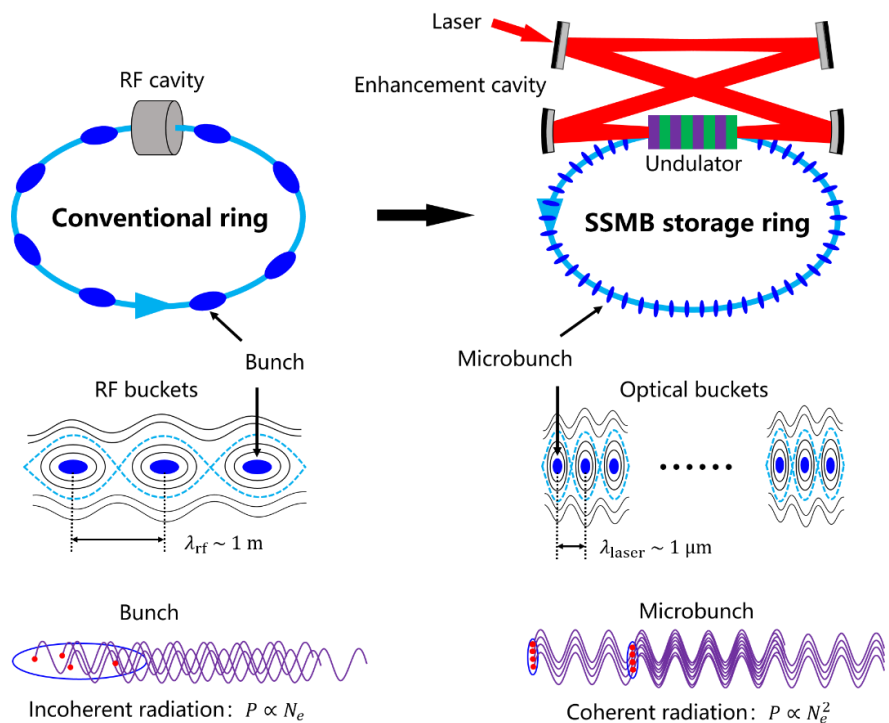


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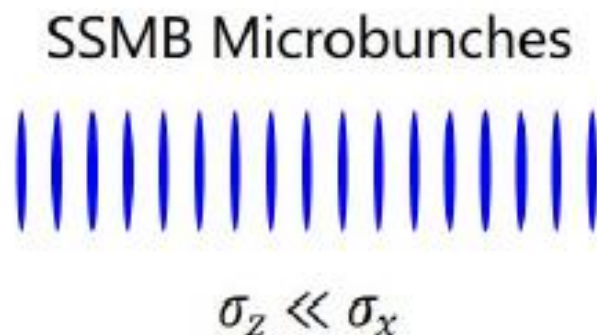
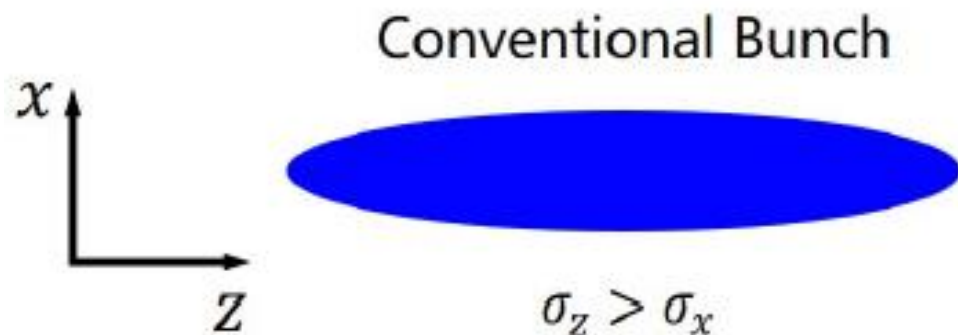
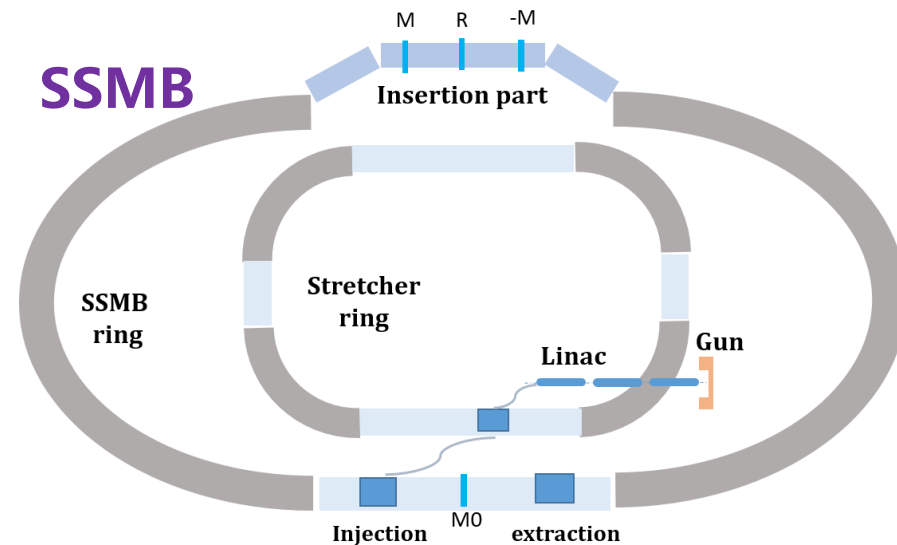
## 6 orders of magnitude extrapolation



- Electron storage ring-based, longitudinal dynamics study needed
- Bunching system **laser modulator**, instead of RF cavity
- Two key points: **Microbunching for strong coherent radiation; turn-by-turn steady state for high repetition rate**

**kW average power EUV radiation for lithography and high flux EUV for ARPES**



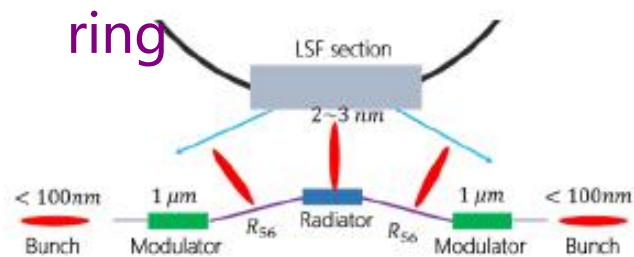


- DLSR: minimize **transverse** size to diffraction limitation
- SSMB: minimize **longitudinal** size for coherent radiation



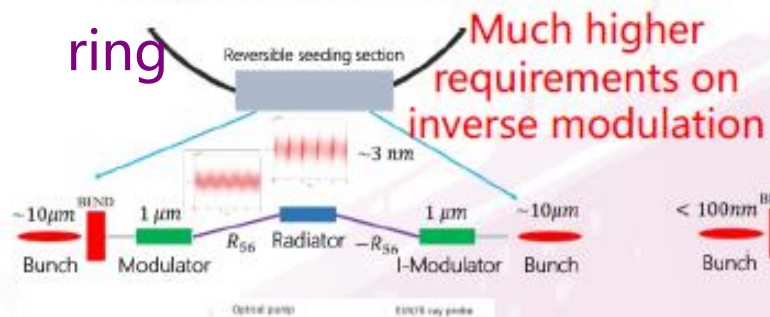


## Longitudinal strong focusing



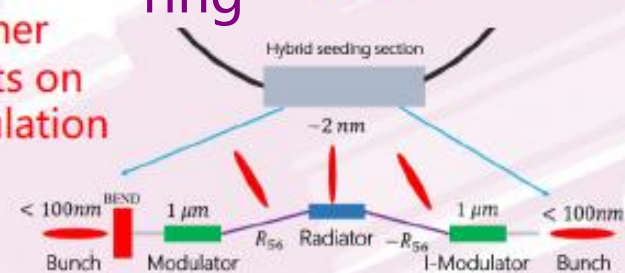
- Low-alpha ring ( $\sim 100$  nm bunch) + LSF( $\sim 3\text{nm}$ )
- Required laser power: hundreds MW, pulsed, Duty rate: 1%
- Pulse power : several kW, average power : several tens W

## Reversible seeding



- normal ring + ADM compress ( $\sim 3\text{nm}$ )
- Required laser power:  $\sim 1$  MW
- Low bunching factor, coasting beam (@10A)
- Average power :  $\sim$  kW

## Hybrid



- Low-alpha ring ( $\sim 100$  nm bunch) + ADM compress ( $\sim 3\text{nm}$ )
- Required laser power:  $\sim 1$  MW
- high bunching factor
- Average power :  $\sim$  kW (@1A)

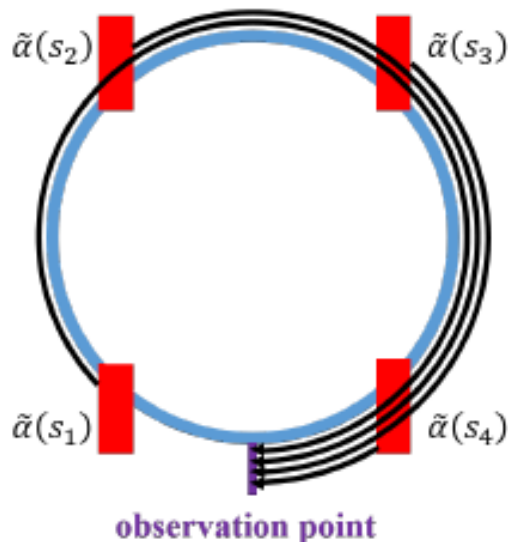
**A low-alpha ring which is very different from normal ring is demanded by SSMB.**



## Existing low-alpha mode ring

- The bunch length in existing low-alpha mode ring: ~1 ps
- There are two reasons why existing ring can't meet SSMB requirements:
  - Wavelength of bunching system
  - Partial alpha effect or local R56

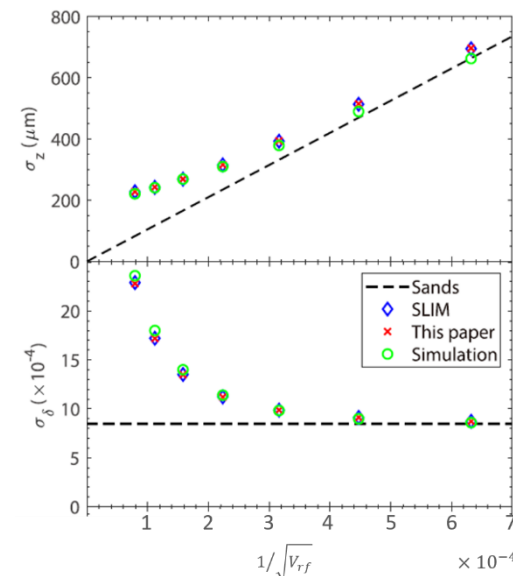
Facilities	Circumference[m]	Achieved alpha
Diamond light source	561.6	$-6 \times 10^{-5}$
Metrology light source	48	$\sim 1 \times 10^{-5}$
BESSY II	240	$7.3 \times 10^{-6}$
SOLEIL	354	$1.7 \times 10^{-5}$
TPS	518.4	$-3 \times 10^{-7}$



$$\tilde{\alpha}(s_j) = \frac{1}{C_0} \int_{s_l}^{\text{observation point}} \frac{\eta(s)}{\rho(s)} ds \quad \sigma_\tau = \sigma_\delta \sqrt{(\alpha_c/\omega_s)^2 + T_0^2 I_{\tilde{\alpha}}}$$

$I_{\tilde{\alpha}}$  the variance of  $\tilde{\alpha}(s_j)$

- The scaling law  $\sigma_z \propto \sqrt{|\eta|}$  breakdown when  $\eta \rightarrow 0$
- The key is to control  $I_{\tilde{\alpha}}$  in low alpha ring





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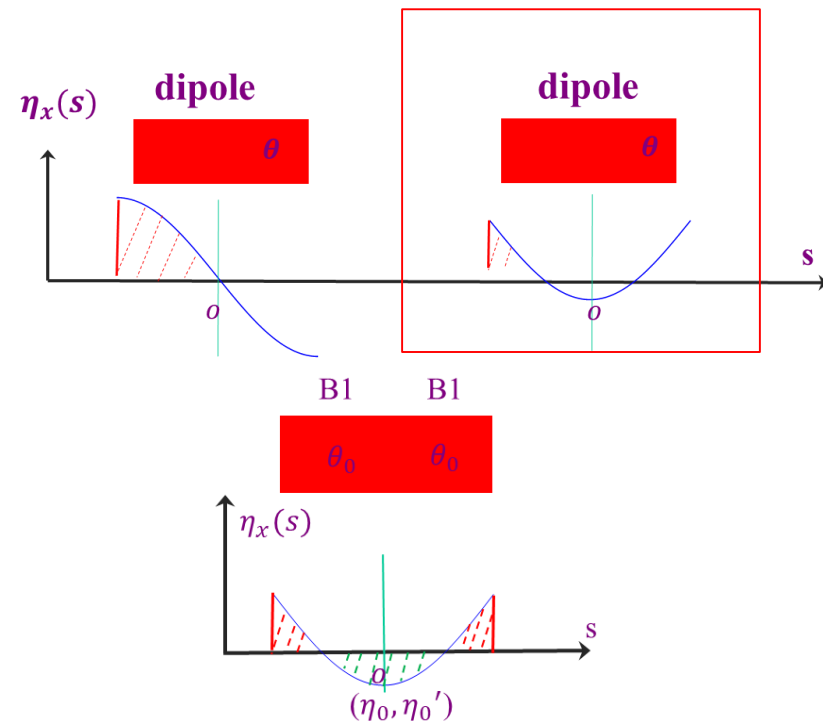
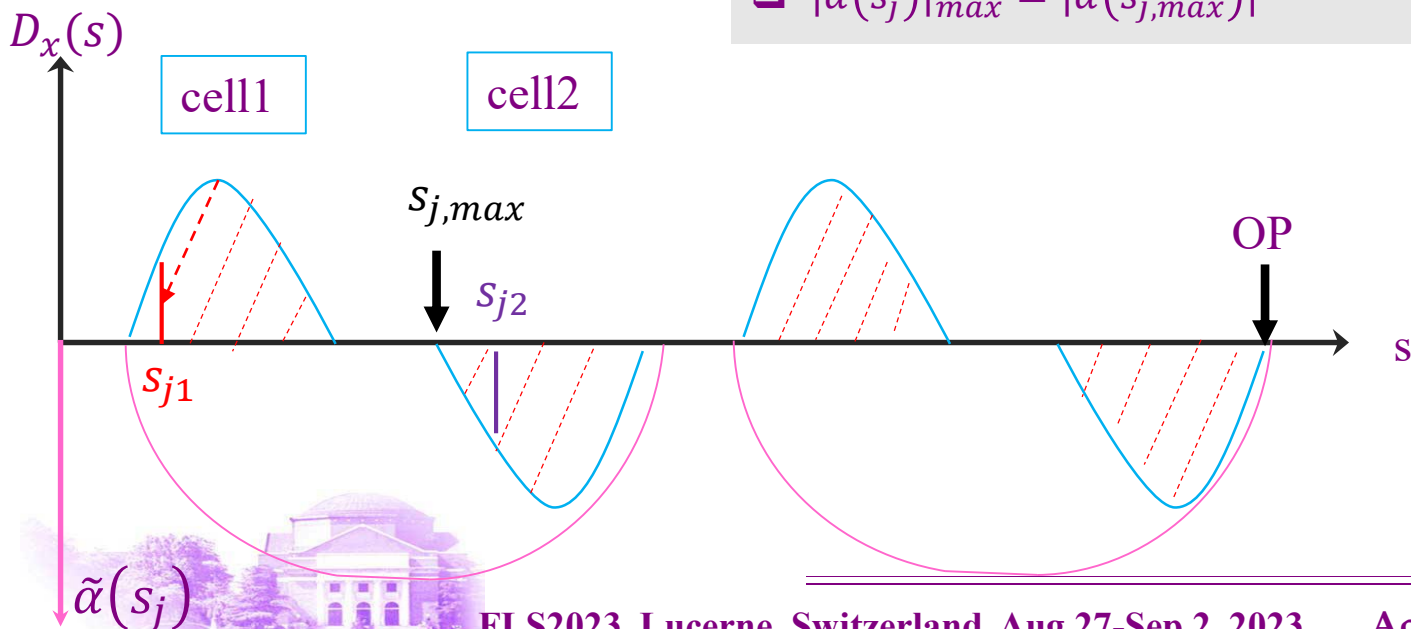


$$\square I_{\tilde{\alpha}} = \left\langle \left( \tilde{\alpha}_{s_j} - \langle \tilde{\alpha}_{s_j} \rangle \right)^2 \right\rangle = \langle \tilde{\alpha}_{s_j}^2 \rangle - \langle 2\tilde{\alpha}_{s_j} \rangle \langle \tilde{\alpha}_{s_j} \rangle + \langle \tilde{\alpha}_{s_j} \rangle^2 = \langle \tilde{\alpha}_{s_j}^2 \rangle - \langle \tilde{\alpha}_{s_j} \rangle^2$$

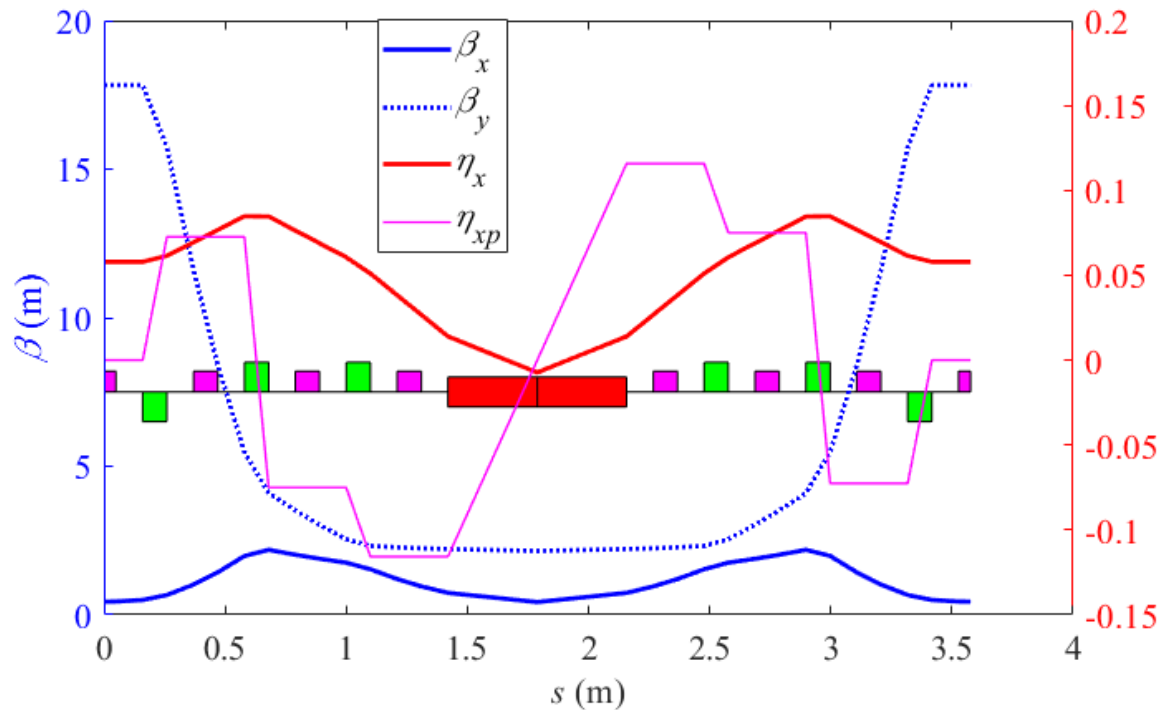
$$\square \tilde{\alpha}(s_j) = \frac{1}{C_0} \int_{s_j}^{OP} \frac{D_x(s)}{\rho(s)} ds$$

- Control the max of dispersion
- The nature idea: make  $\alpha_c \sim 0$  in each dipole

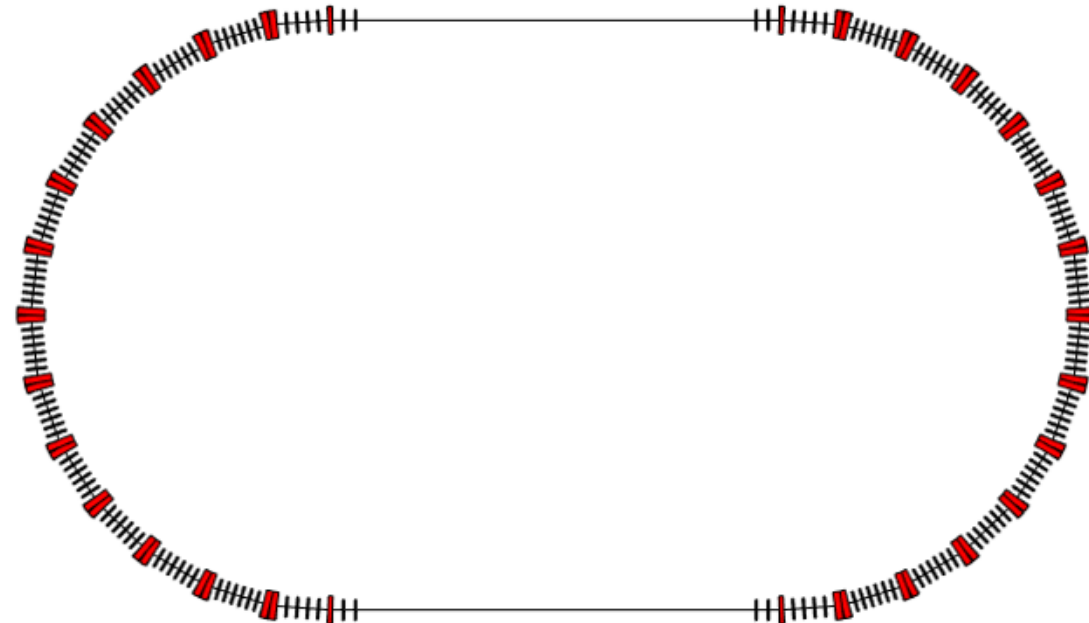
- $R_{56,c} = R_{56,1} + R_{56,2} \sim 0$
- So  $\tilde{\alpha}(s_j) < 0$  for all radiation points
- $|\tilde{\alpha}(s_j)|_{min} = 0$
- $|\tilde{\alpha}(s_j)|_{max} = |\tilde{\alpha}(s_{j,max})|$



- Make the  $\alpha_c$  in each dipole be 0
- $\eta_0'$  at the middle of the dipole is 0
- We get  $\eta_0 = \rho \frac{(\sin(\theta_0) - \theta_0)}{\sin(\theta_0)} \approx -\frac{1}{6} \rho \theta_0^2$ , and  $\eta(\theta_0) = \frac{1}{3} \rho \theta_0^2$



Main Cell



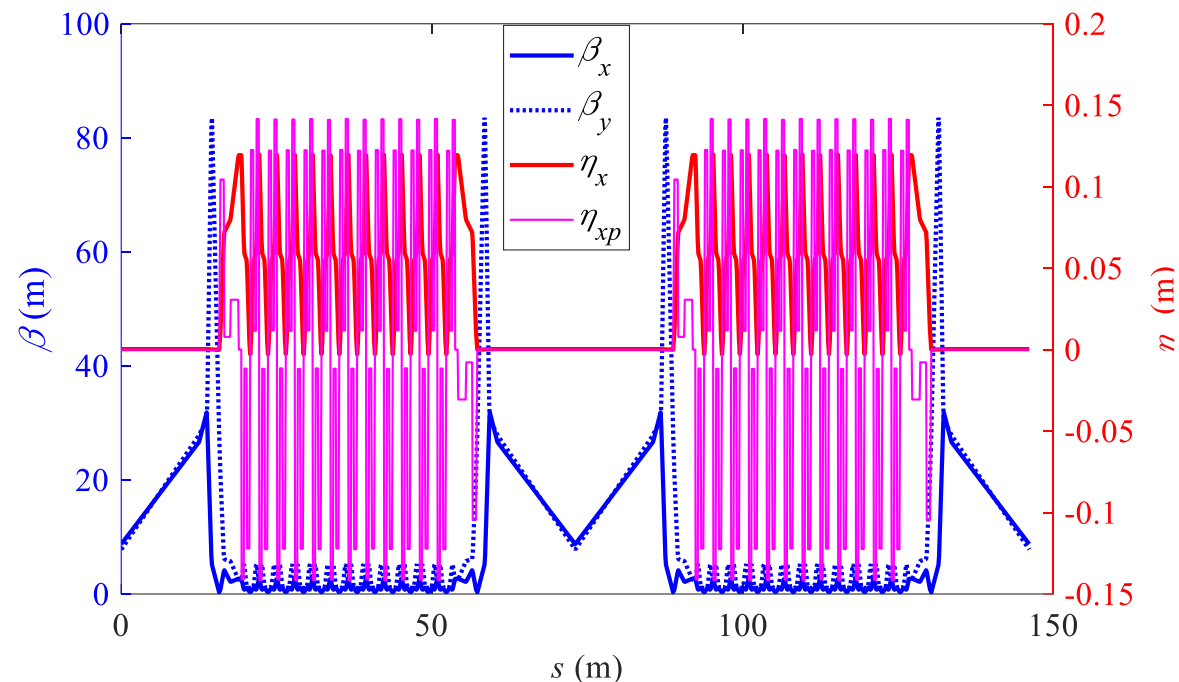
Ring layout

Tune:  $\frac{i}{n}, \frac{j}{n}$ , in this lattice  $n=12$ , tune  $(\frac{7}{12}, \frac{3}{12})$

Dispersion in middle point:  $-\frac{1}{6}\rho\theta_0^2$



Parameters	Value	Units
Circumference	143.78	m
Beam energy	400	MeV
Tunes x/y	18.58/7.11	/
Phase slippage factor	2.69e-6	/
2nd order phase slippage factor	1.23e-4	/
Natural emittance	281.7	pm
LM wavelength	1	$\mu\text{m}$
LM voltage	100	kV
Energy spread	$2.23 \times 10^{-4}$	/
Bunch length at straight	91.4	nm
Damping times (x/y/z)	191.3/191.3/96.5	ms
Energy loss per turn	0.71	keV



Twiss of ring

The bunch length at straight is less than 100 nm



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- Destroy RF bucket if too large

$$\alpha = \alpha_c + \alpha_2 \delta + \dots$$

$$\alpha_{c2} = \frac{1}{C} \int_0^C \left( \frac{\eta_2}{\rho} + \frac{\eta_1'^2}{2} \right) ds$$

when  $|\alpha_2| > \alpha_{2Cr}$ , the RF bucket will transmit to  $\alpha$ -bucket, bucket area will shrink

$$\alpha_{2Cr} = \sqrt{\frac{E_0 h |\alpha_1|^3}{12 e V_{rf} [-\cos \varphi_s + (\frac{\pi}{2} - \varphi_s) \sin(\varphi_s)]}}$$

$$\eta_2(s) = -\eta_1(s) + \frac{1}{2 \sin \pi Q_x} * \int_s^{s+C} \sqrt{\beta_x(s) \beta_x(\sigma)} \cos(\pi Q_x - \mu_{\sigma s}) * \left( K_1(\sigma) \eta_1(\sigma) - \frac{1}{2} K_2(\sigma) \eta_1^2(\sigma) \right) d\sigma$$

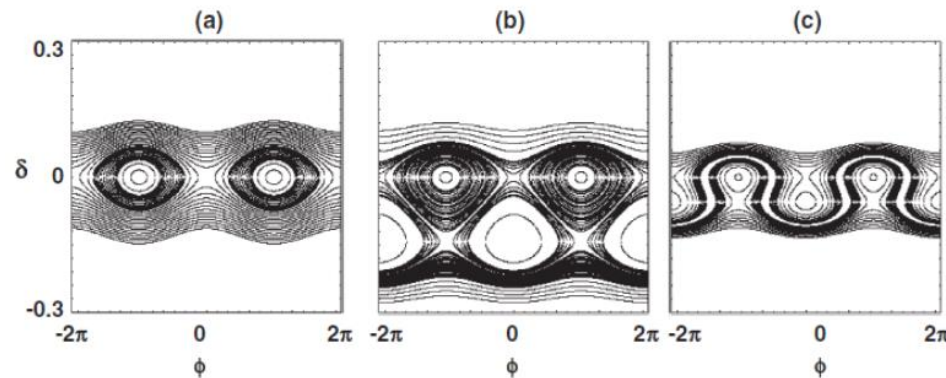
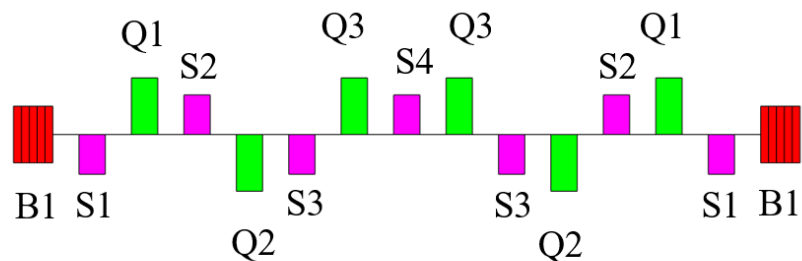


Fig. 8. Effect of second-order momentum compaction factor on longitudinal phase space in ring. The first-order momentum compaction factor in (a), (b), and (c) is  $2.2 \times 10^{-3}$ . The second-order momentum compaction factors in (a), (b), and (c) are 0.006, 0.02311, and 0.06, respectively.

The sextupoles should be located at dispersive location to correct chromaticities for three directions, at least three families needed.

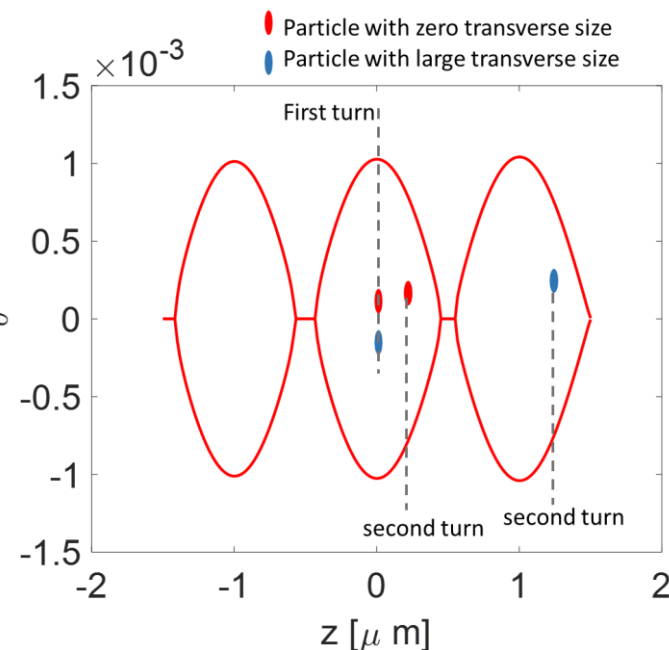
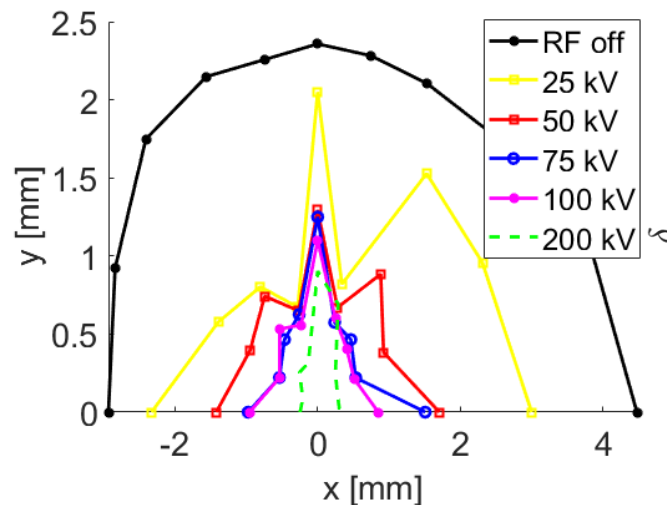


- ◆ Sextupoles are inserted in main cell for chromaticity and  $\alpha_2$  correction



Main cell

- Bucket width will be  $1 \mu\text{m}$  in SSMB ring
- The path length oscillation amplitude by transverse longitudinal coupling can be larger than  $1 \mu\text{m}$  easily.
- Particles with large transverse size will jump in different buckets and make longitudinal motion become unstable







- Define the Hamiltonian as (under 3rd order, omit longitudinal Hamiltonian)

$$H(J_x, J_y, \delta) = \mu_x J_x + \mu_y J_y + h_{11001} J_x \delta + h_{00111} J_y \delta + |h_{20001}| J_x \delta e^{-2\phi_x j} + |h_{00201}| J_y \delta e^{-2\phi_y j}$$

- So we can get path length deviation from T-L coupling (linear dispersion not discussed)

$$\Delta z = \frac{\partial H}{\partial \delta} = h_{11001} J_x + h_{00111} J_y + |h_{20001}| J_x e^{-2\phi_x j} + |h_{00201}| J_y e^{-2\phi_y j}$$

- From J. Bengtsson

$$h_{11001} = \frac{1}{4} \sum_{i=1}^N [(b_2 L)_i - 2(b_3 L)_i \eta_{xi}] \beta_{xi}$$

$$h_{00111} = -\frac{1}{4} \sum_{i=1}^N [(b_2 L)_i - 2(b_3 L)_i \eta_{xi}] \beta_{yi}$$

$$h_{20001} = \frac{1}{8} \sum_{i=1}^N [(b_2 L)_i - 2(b_3 L)_i \eta_{xi}] \beta_{xi} e^{j2\mu_{xi}}$$

$$h_{00201} = -\frac{1}{8} \sum_{i=1}^N [(b_2 L)_i - 2(b_3 L)_i \eta_{xi}] \beta_{yi} e^{j2\mu_{yi}}$$

- We can get more accurate expression as

$$\Delta z_n = T_{511} x_n^2 + T_{512} x_n x_n' + T_{522} x_n'^2 \quad x_n = \sqrt{2\beta_x J_x} \cos(2\pi \nu_x n + \phi_0)$$

$$x_n' = -\sqrt{\frac{2J_x}{\beta_x}} (\alpha_x \cos(2\pi \nu_x n + \phi_0) + \sin(2\pi \nu_x n + \phi_0))$$

$$\Delta z = (\beta_x T_{511} - \alpha_x T_{512} + \gamma_x T_{522}) J_x + A_x J_x \sin(4\pi \nu_x n + \psi_A)$$

$$A_x^2 = \beta_x^2 T_{511}^2 + \beta_x \gamma_x T_{512}^2 + \gamma_x^2 T_{522}^2 - 2\alpha_x (\beta_x T_{511} + \gamma_x T_{522}) T_{512} + 2(\alpha_x^2 - 1) T_{511} T_{522}$$

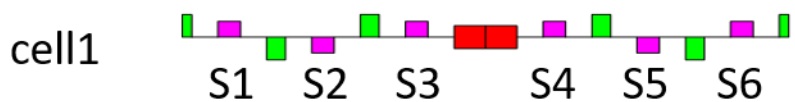
$$h_{11001} = 2\pi \xi_x = \beta_x T_{511} - \alpha_x T_{512} + \gamma_x T_{522}$$

$$h_{20001} = \sqrt{\beta_x^2 T_{511}^2 + \beta_x \gamma_x T_{512}^2 + \gamma_x^2 T_{522}^2 - 2\alpha_x (\beta_x T_{511} + \gamma_x T_{522}) T_{512} + 2(\alpha_x^2 - 1) T_{511} T_{522}}$$

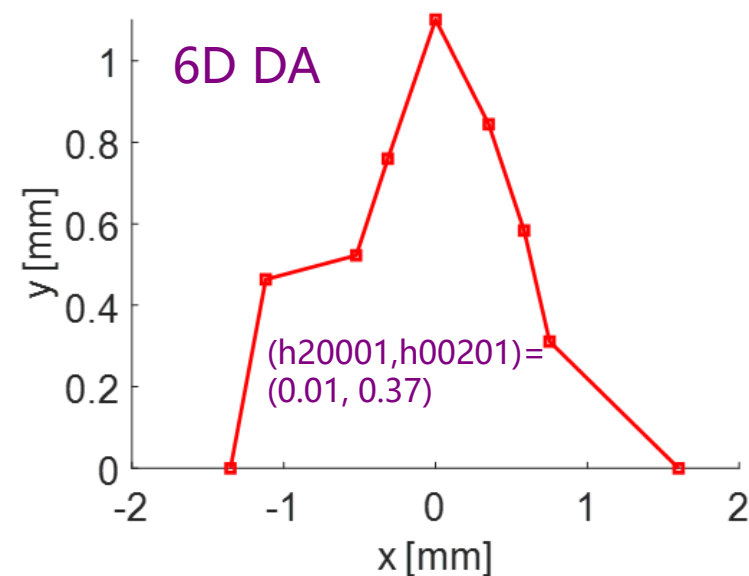
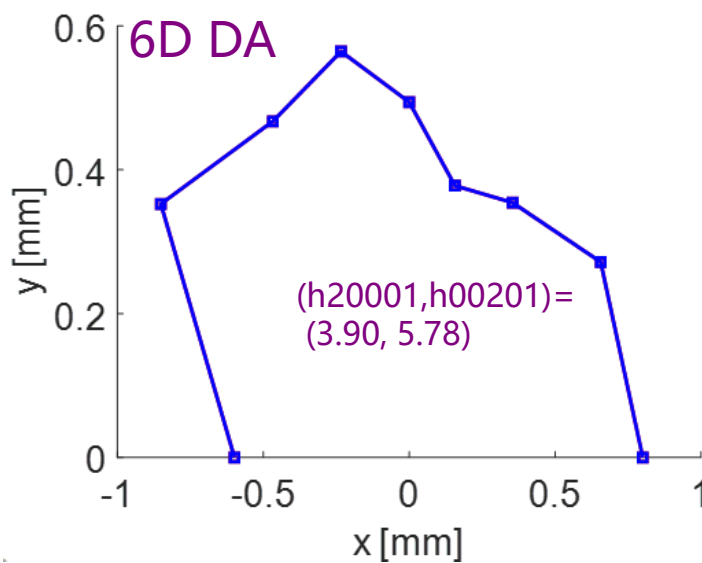




- According to J. Bengtsson's formula, we have no knobs to control the  $h_{20001}$  and  $h_{00201}$  if sextupoles are all used periodically.
- We can break the period by the layout below



By adjust  $k_1$  and  $k_2$ , we can optimize  $(h_{20001}, h_{00201})$  from  $(3.90, 5.78)$  to  $(0.01, 0.37)$





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- We have done the analysis for partial alpha effects in low alpha ring, and proposed a method to minimize it.
- Based on the analysis, the linear lattice is designed, bunch length under 100 nm can be hold in the ring.
- We have done some preliminary studies on the nonlinear optimization for this kind of storage ring, the 6-D DA will be limited by T-L coupling, which has been optimized by specialized sextupole scheme.





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# Thanks for your attention!

# Comments are appreciated!

